

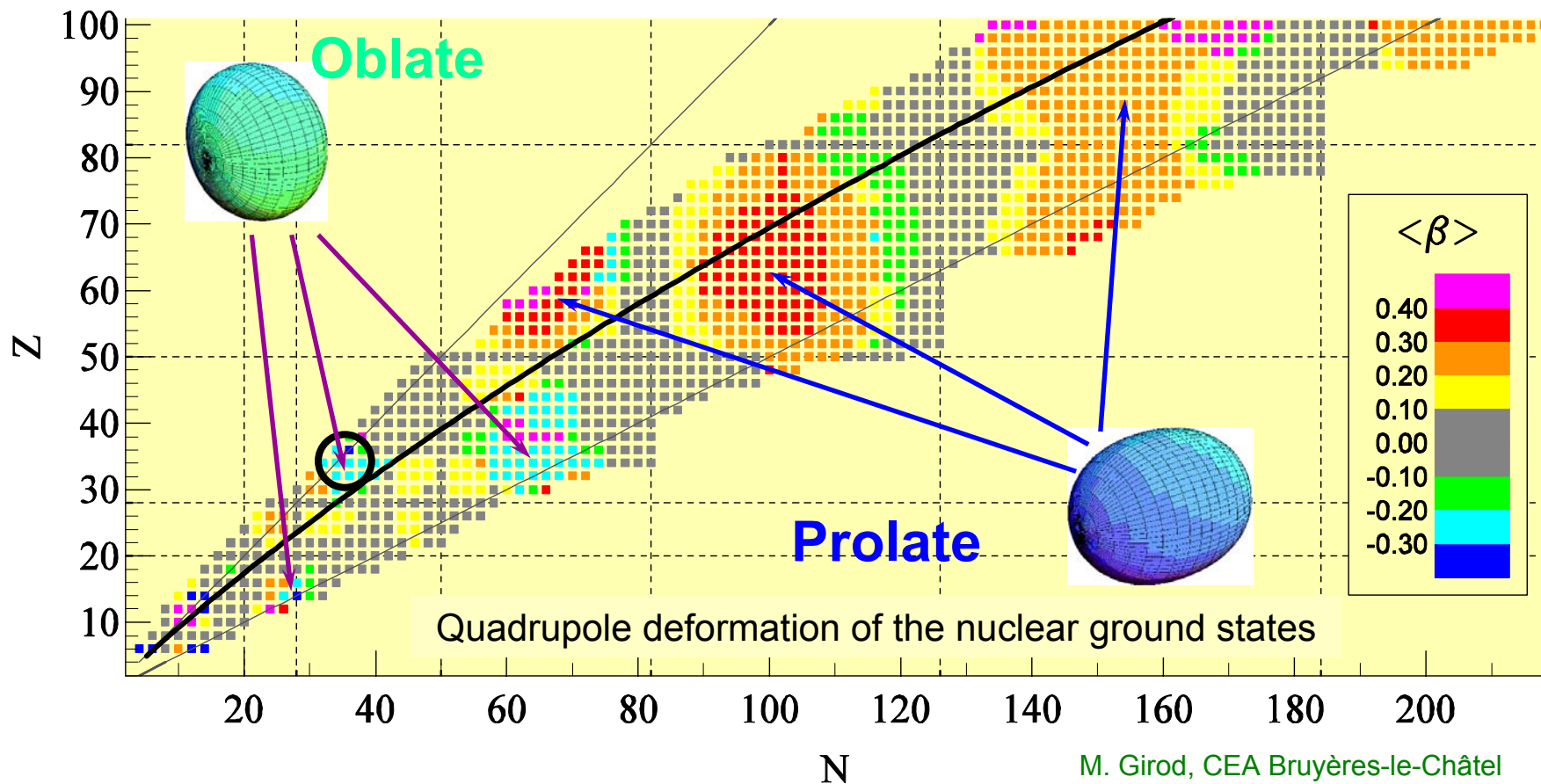
# Shape coexistence in light Krypton isotopes

- Introduction : Shape coexistence
- “Safe” Coulomb excitation of RIBs
- RDDS Lifetime measurement
- Results and conclusions

Andreas G3rger

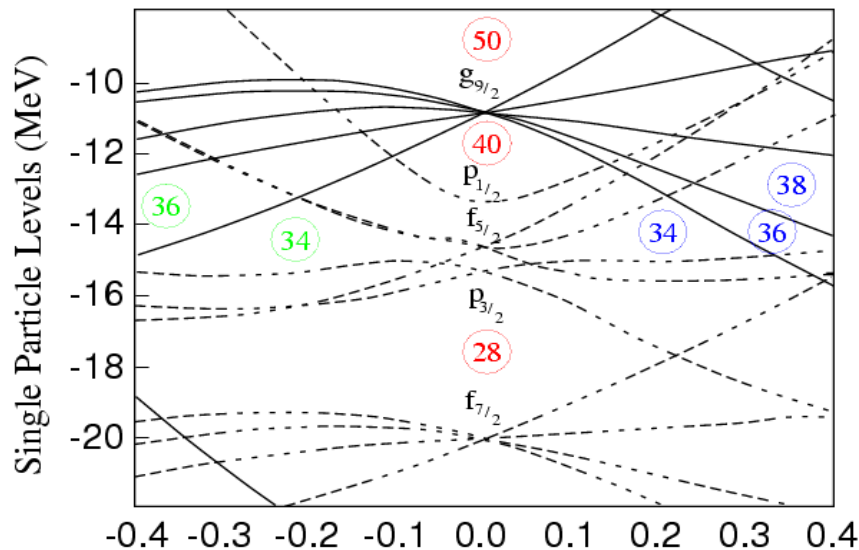
*DAPNIA / Service de Physique Nucl3eaire  
Commissariat 3 l'3nergie Atomique, Saclay*

# Shapes of atomic nuclei

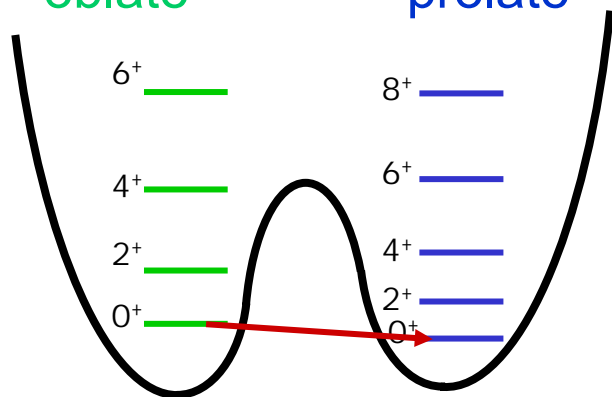


- oblate ground states predicted for  $A \sim 70$  near  $N=Z$
- prolate and oblate states within small energy range  
⇒ **shape coexistence**

# Shape coexistence



oblate  $\beta$  prolate



Shape isomer, **E0 transition**

$$\text{Configuration mixing: } |\psi(0_1^+)\rangle = a|\varphi_{pro}\rangle + b|\varphi_{obl}\rangle$$

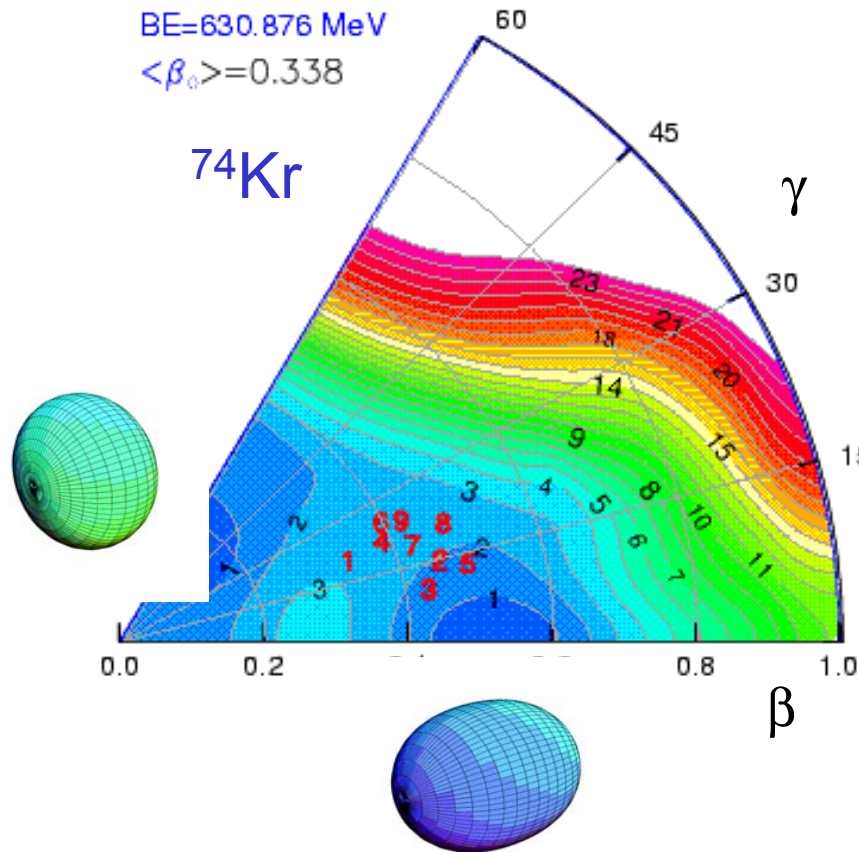
$$|\psi(0_2^+)\rangle = a|\varphi_{obl}\rangle - b|\varphi_{pro}\rangle$$

shape coexistence expected in

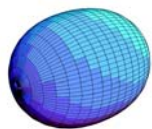


BE=630.876 MeV  
 $\langle\beta_0\rangle=0.338$

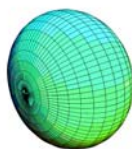
${}^{74}\text{Kr}$



# Systematics of the light krypton isotopes

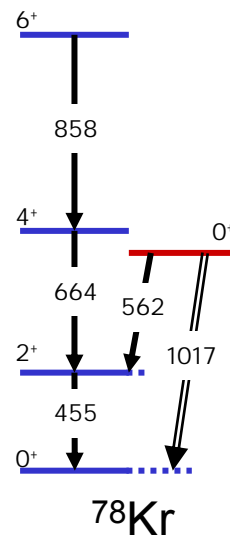
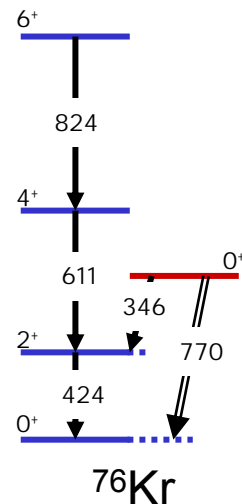
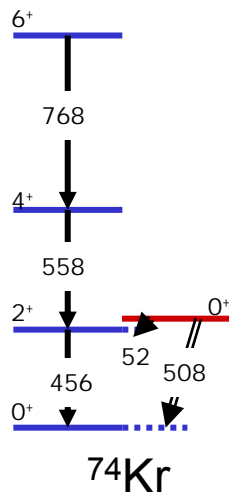
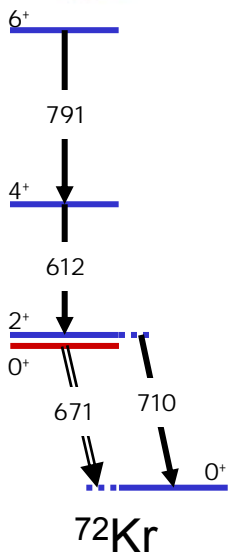


prolate



oblate

- energy of excited  $0^+$
- E0 strengths  $\rho^2(E0)$
- configuration mixing
- Inversion of ground state shape for  $^{72}\text{Kr}$
- Coulomb excitation to determine the nuclear shapes directly

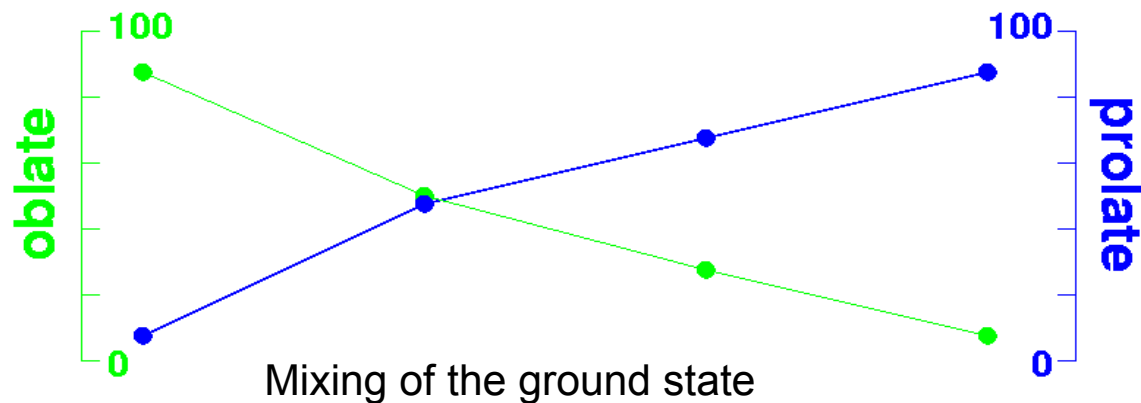


$\rho^2(E0)$   $72 \cdot 10^{-3}$

$85 \cdot 10^{-3}$

$79 \cdot 10^{-3}$

$47 \cdot 10^{-3}$



E. Bouchez et. al.,  
Phys. Rev. Lett. 90, 082502 (2003)

# Shape coexistence in light Krypton isotopes

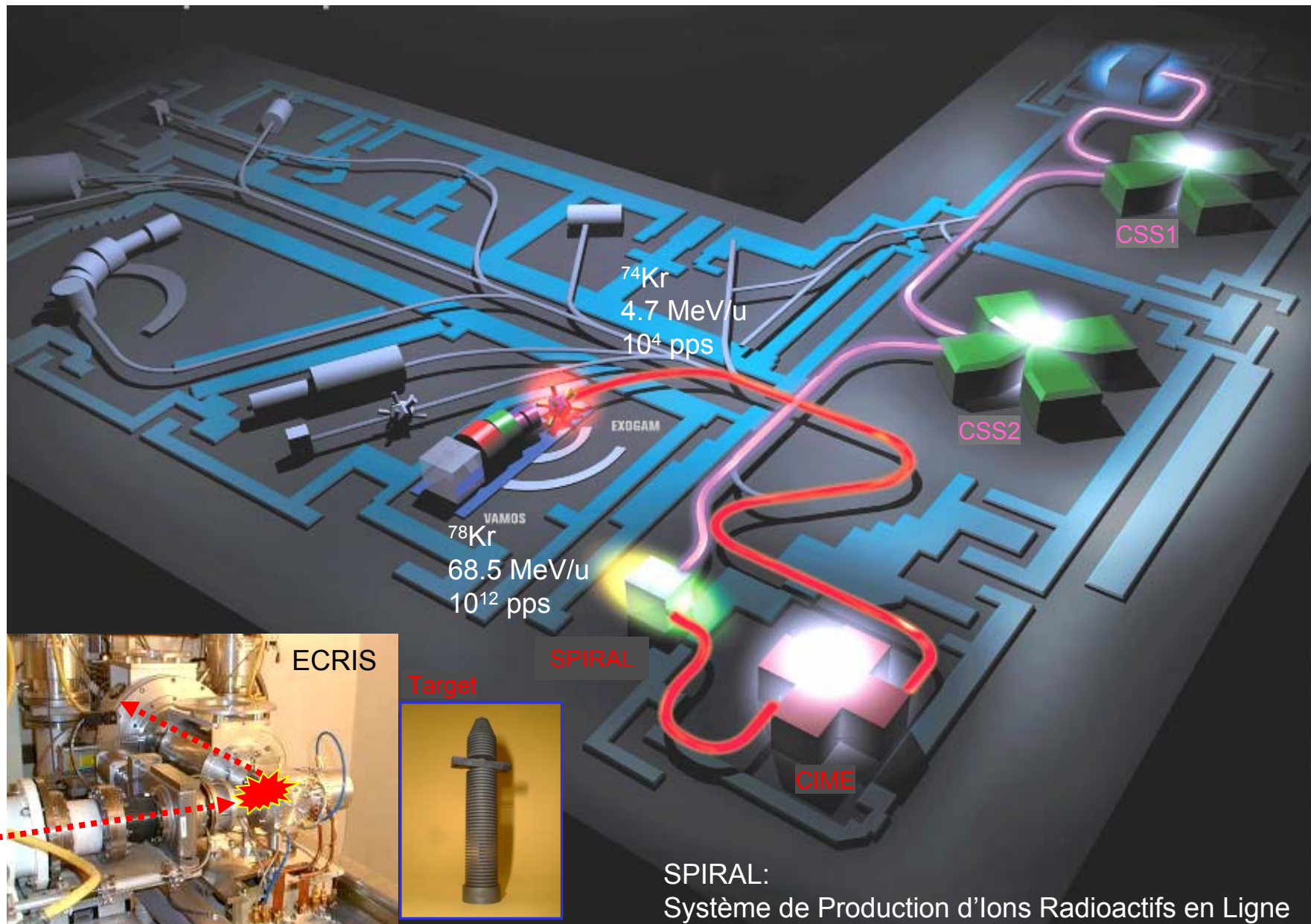
- Introduction : Shape coexistence
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# Radioactive beam production: SPIRAL

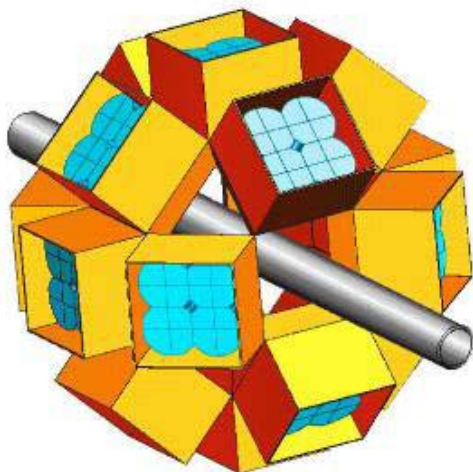
dapnia  
SPHn

cea

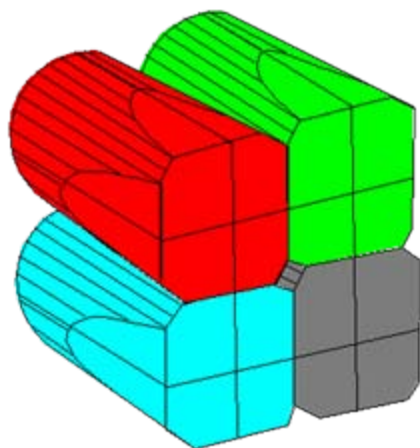
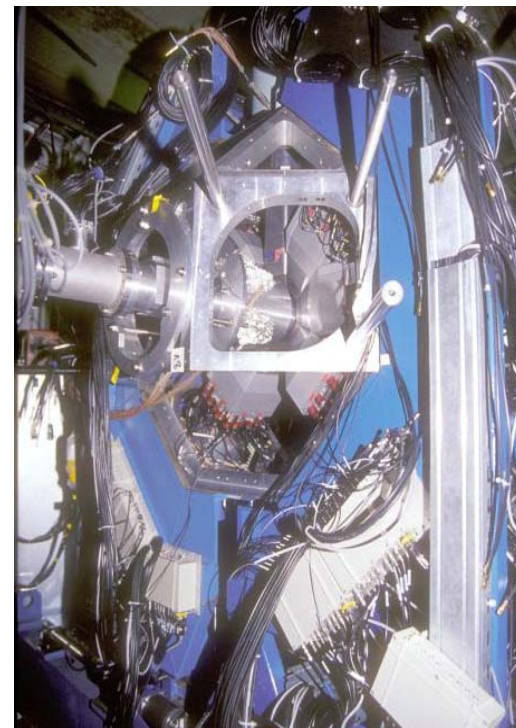
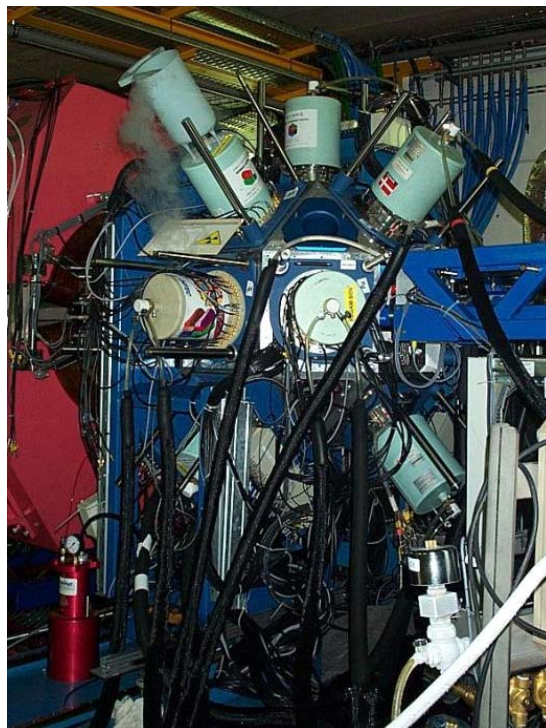
saclay



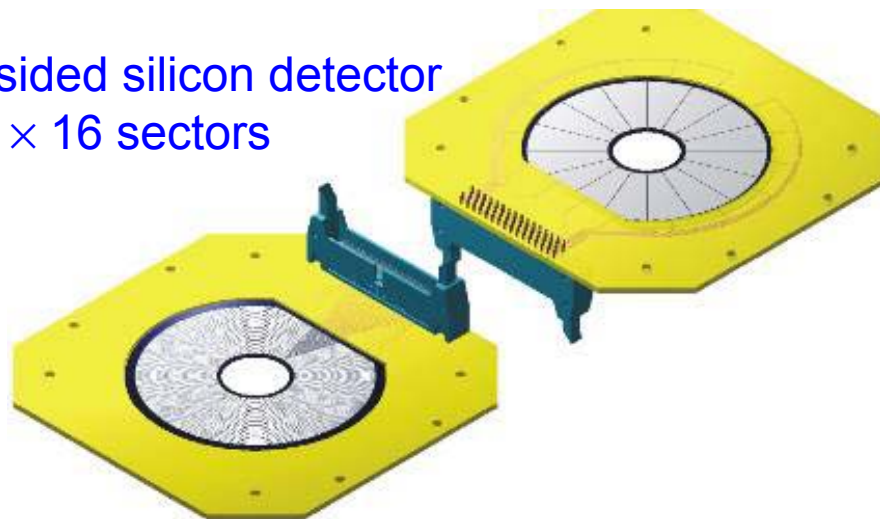
# EXOGAM



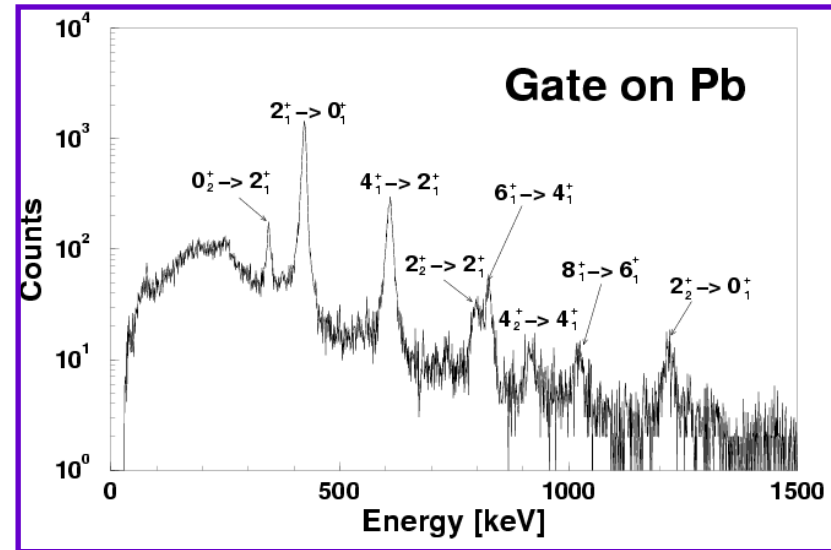
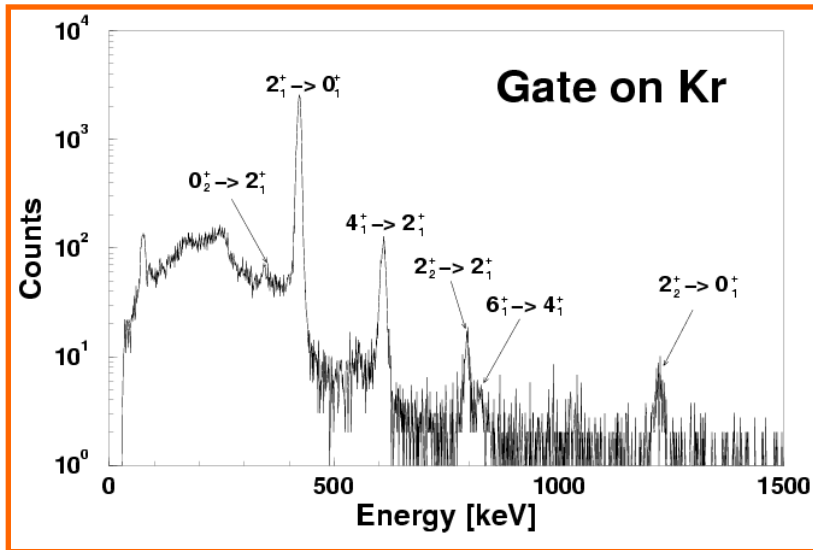
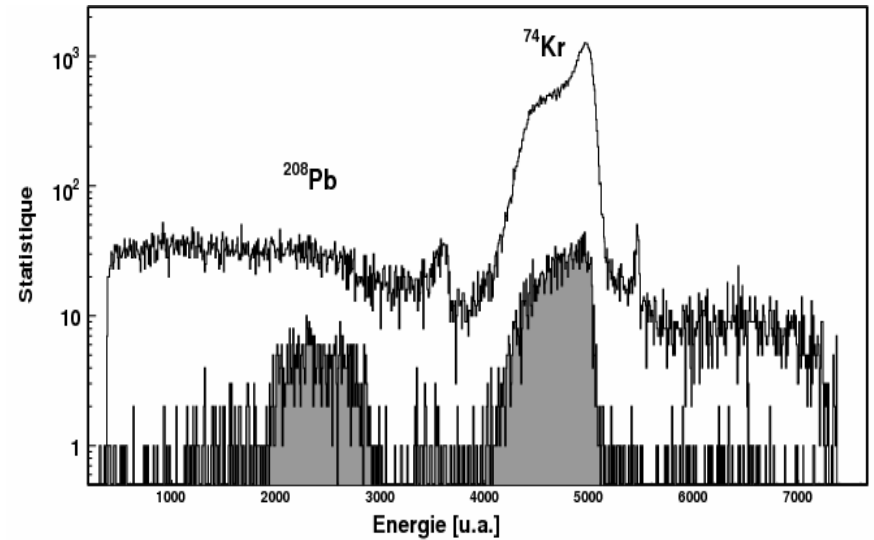
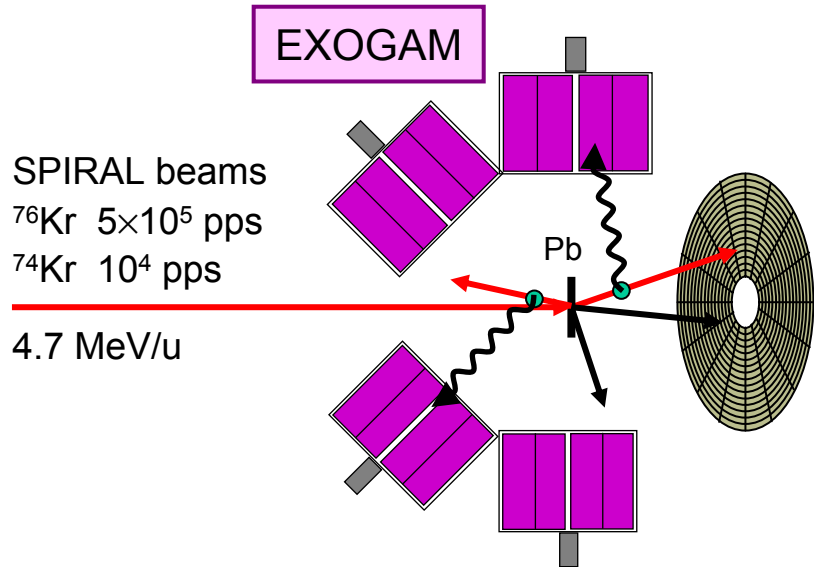
16 large Ge Clover detectors  
4 × 4 segmented



Double-sided silicon detector  
48 rings × 16 sectors



# Coulomb excitation of $^{74}\text{Kr}$ and $^{76}\text{Kr}$



Acta Phys. Pol. B 36, 1281 (2005)

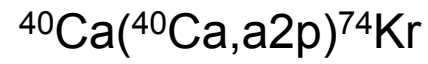
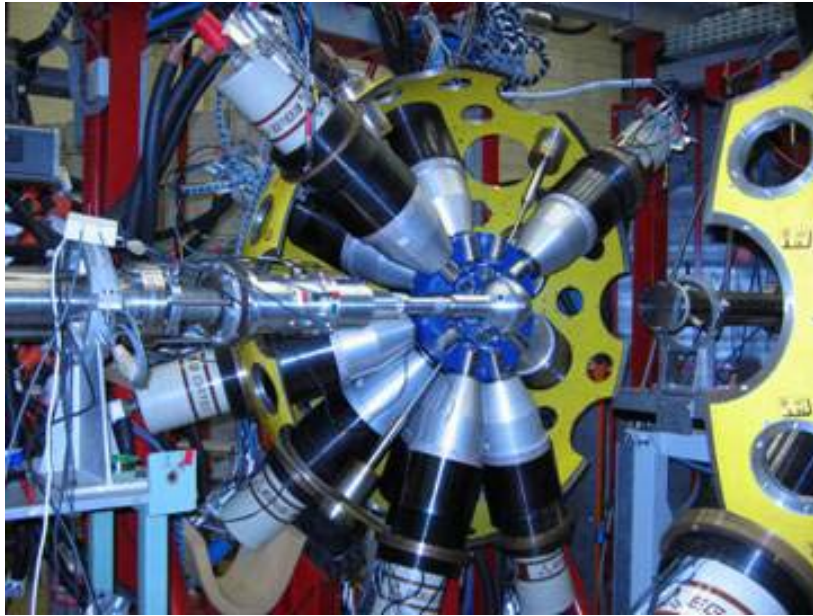




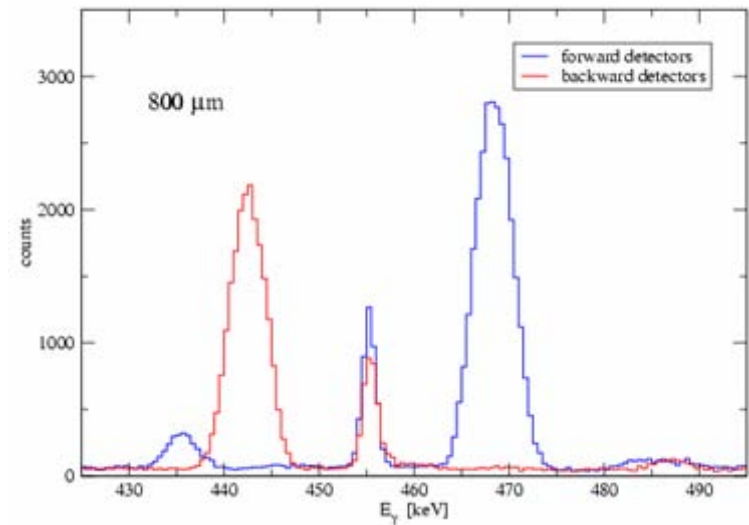
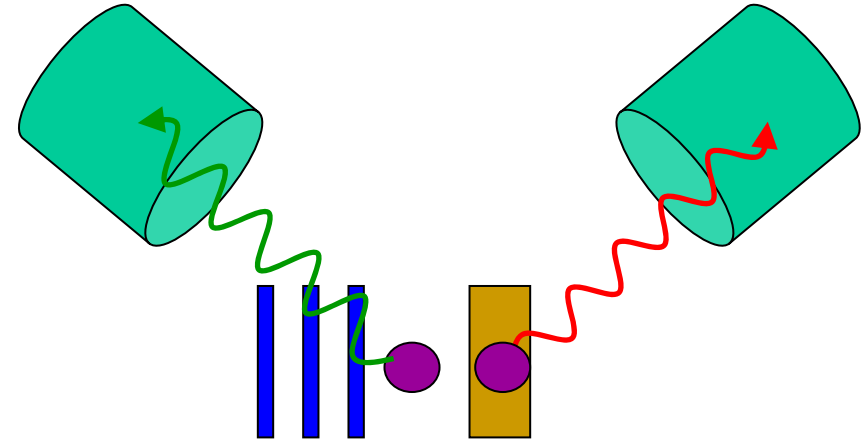
# Shape coexistence in light Krypton isotopes

- Introduction : Shape coexistence
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# Lifetime measurement with GASP and the Köln Plunger



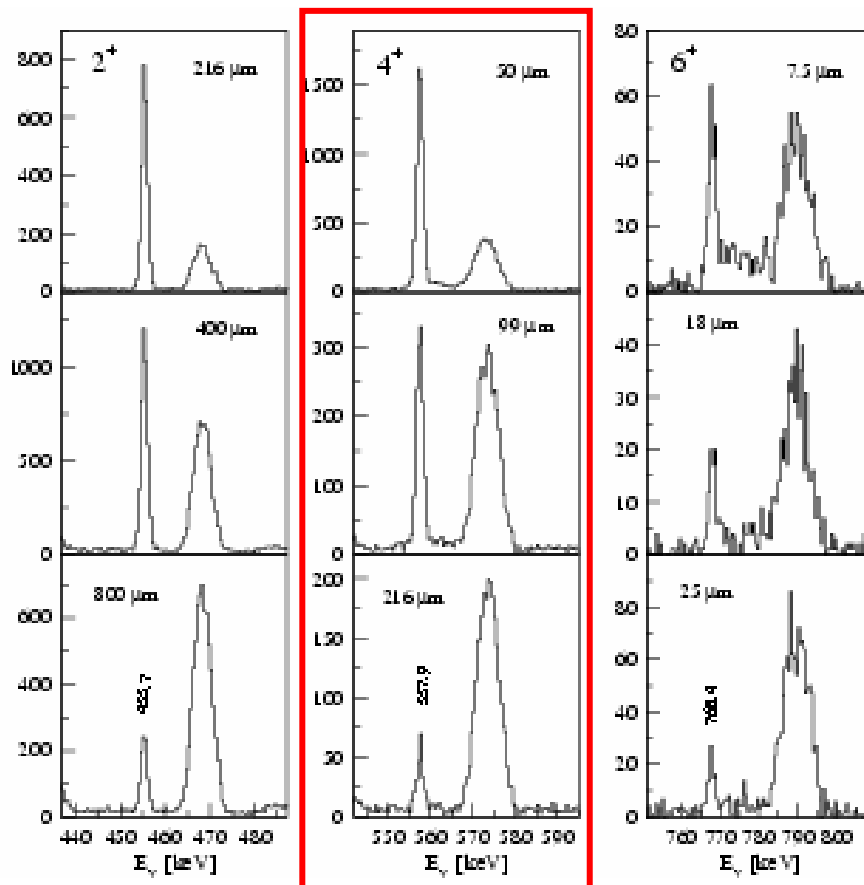
124 MeV



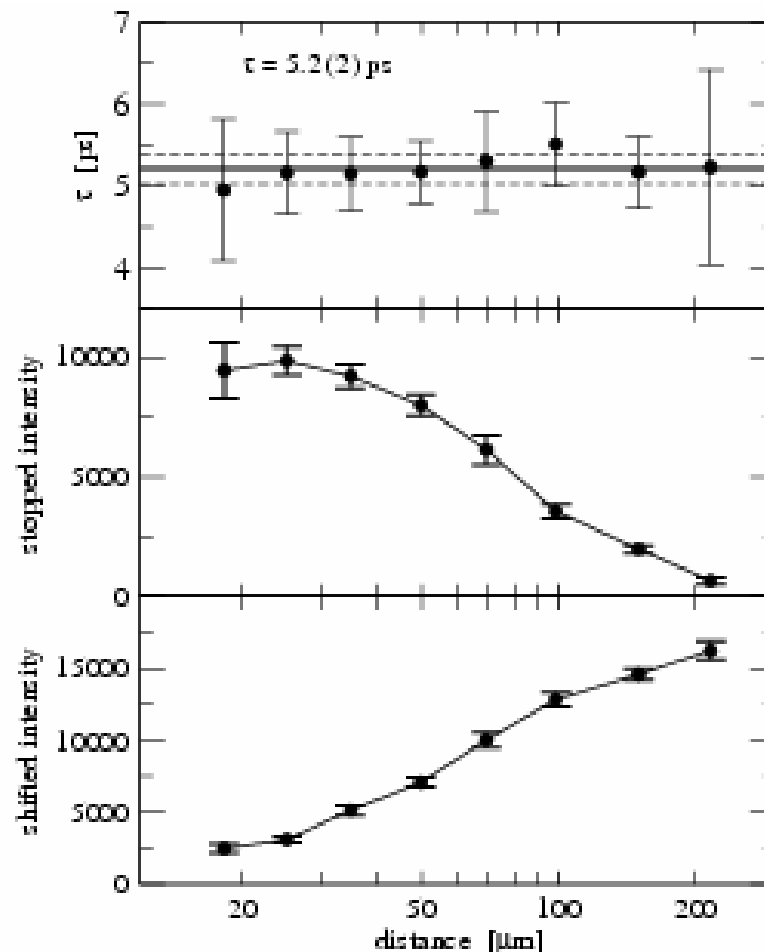
# Differential decay curve method

$^{74}\text{Kr}$

- forward detectors ( $36^\circ$ )
- gated from above



Example:  $^{74}\text{Kr}$ ,  $4^+$ ,  $36^\circ$

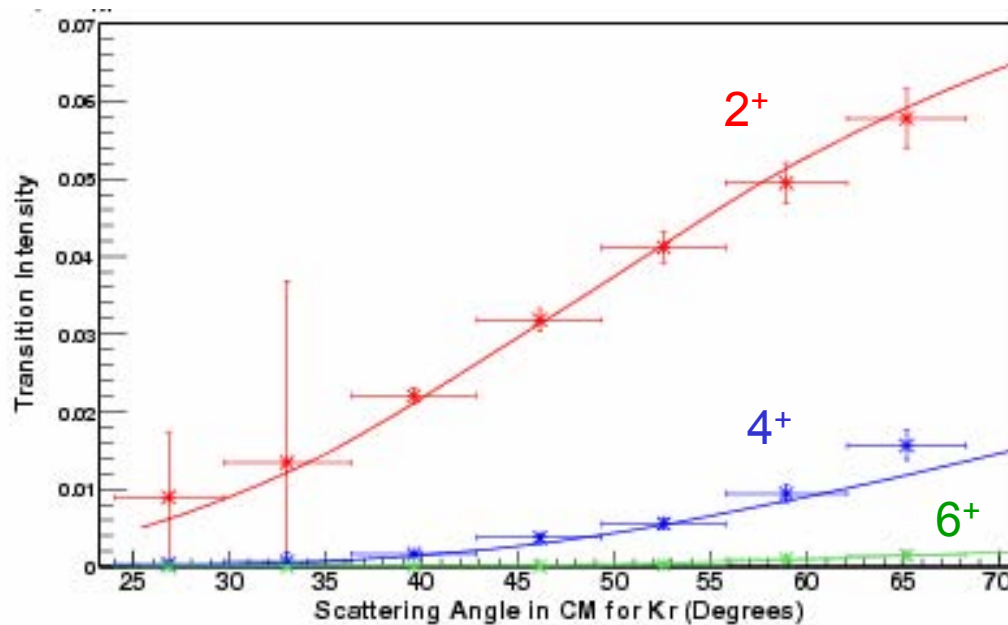


Eur. Phys. J. A 26, 153 (2005)

# Lifetime results

Eur. Phys. J. A 26, 153 (2005)

$^{74}\text{Kr}$	$2^+$	$4^+$	$^{76}\text{Kr}$	$2^+$	$4^+$
new	33.8(6)	5.2(2)	new	41.5(8)	3.67(9) [ps]
	28.8(57)	13.2(7)		35.3(10)	4.8(5) [ps]
	J. Roth et al., J.Phys.G, L25 (1984)			B. Wörmann et al., NPA 431, 170 (1984)	



Results consistent with transition probabilities from Coulomb excitation.

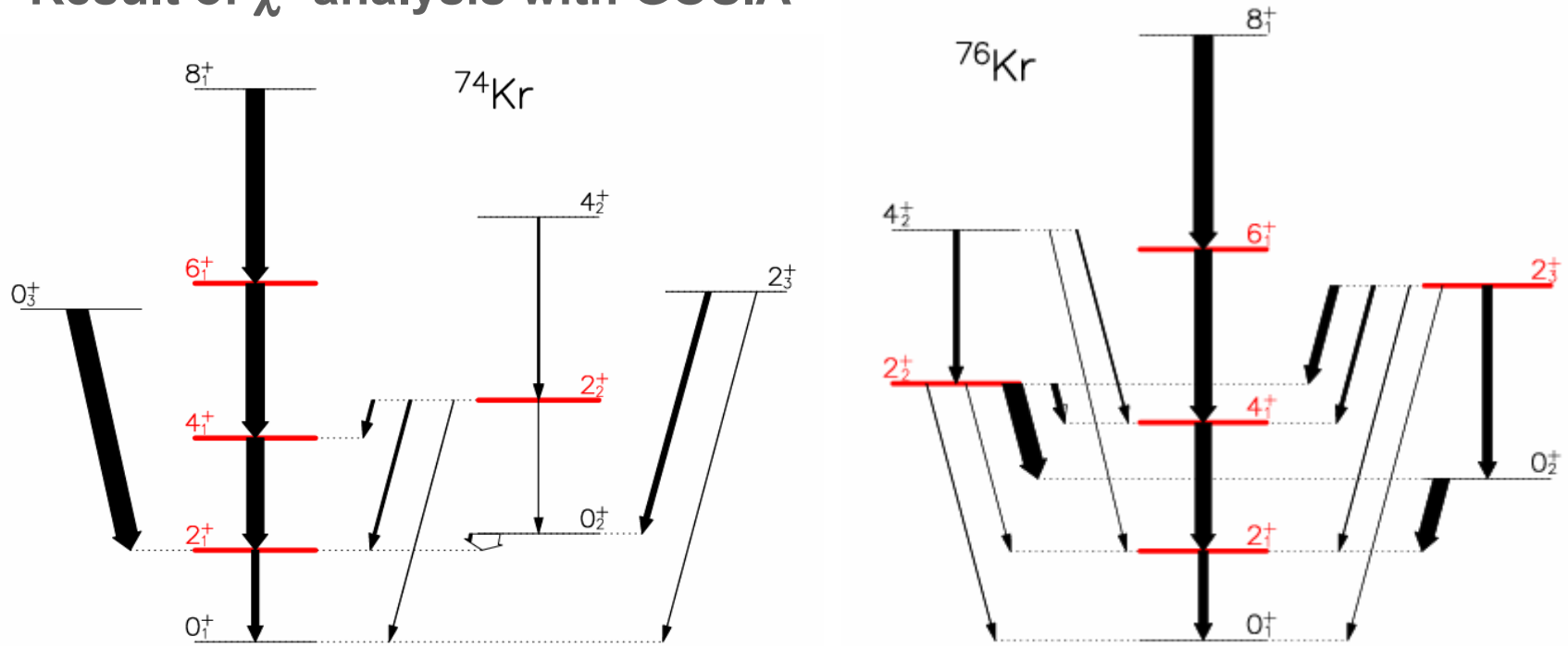
Lifetimes used to constrain GOSIA fit.

⇒ enhanced sensitivity for non-yrast transitions and diagonal matrix elements

# Shape coexistence in light Krypton isotopes

- Introduction : Shape coexistence
- “Safe” Coulomb excitation of RIBs
- RDDS Lifetime measurement
- **Results and conclusions**

# Result of $\chi^2$ analysis with GOSIA



➤ 14 transitional E2 matrix elements

➤ 18 transitional E2 matrix elements

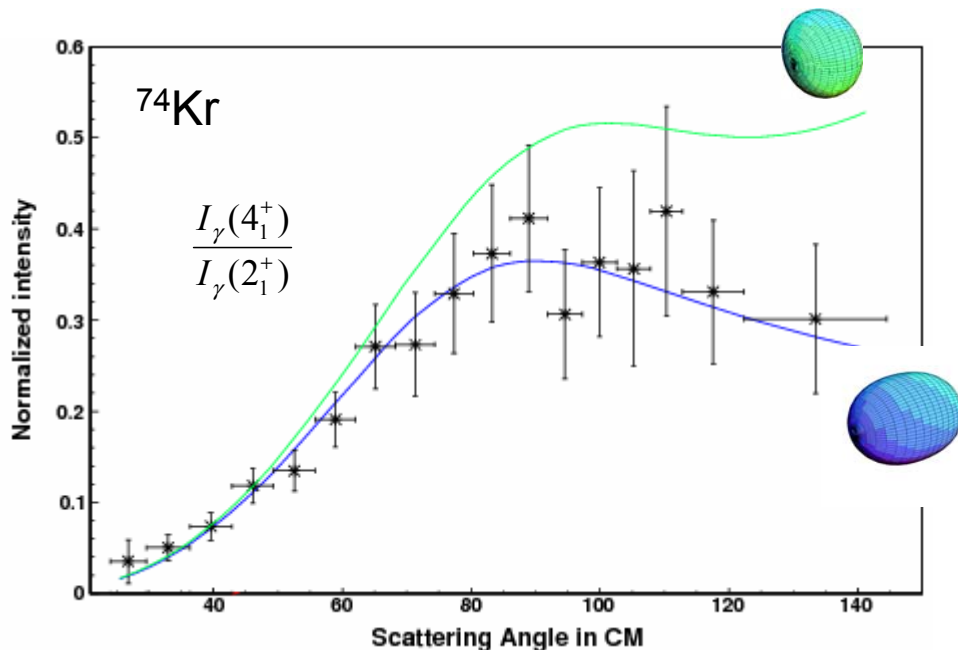
$$B(E2) = \frac{\left| \langle I_f \| \mathbf{M}(E2) \| I_i \rangle \right|^2}{2I_i + 1}$$

➤ 4 diagonal E2 matrix elements

➤ 5 diagonal E2 matrix elements

$$eQ_0 = \sqrt{\frac{16\pi}{5}} \frac{1}{\sqrt{2I+1}} \frac{\langle I \| \mathbf{M}(E2) \| I \rangle}{\langle I020 | I0 \rangle}$$

# Sensitivity to quadrupole moments



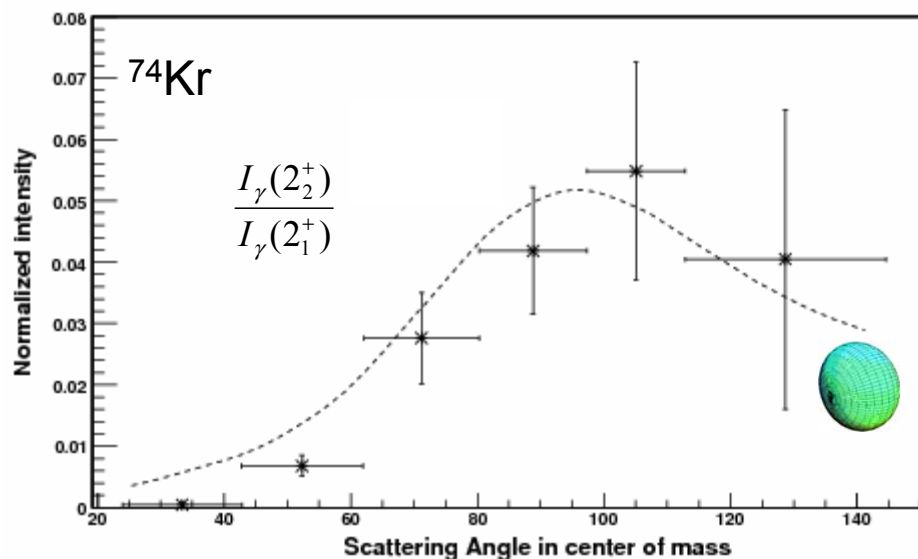
full  $\chi^2$  minimization:

$$\langle 2_1^+ \| \mathbf{M}(E2) \| 2_1^+ \rangle = -0.70_{-0.30}^{+0.33}$$

$$\langle 4_1^+ \| \mathbf{M}(E2) \| 4_1^+ \rangle = -1.02_{-0.21}^{+0.59}$$

negative matrix element  
(positive quadrupole moment  $Q_0$ )

$\Rightarrow$  prolate shape



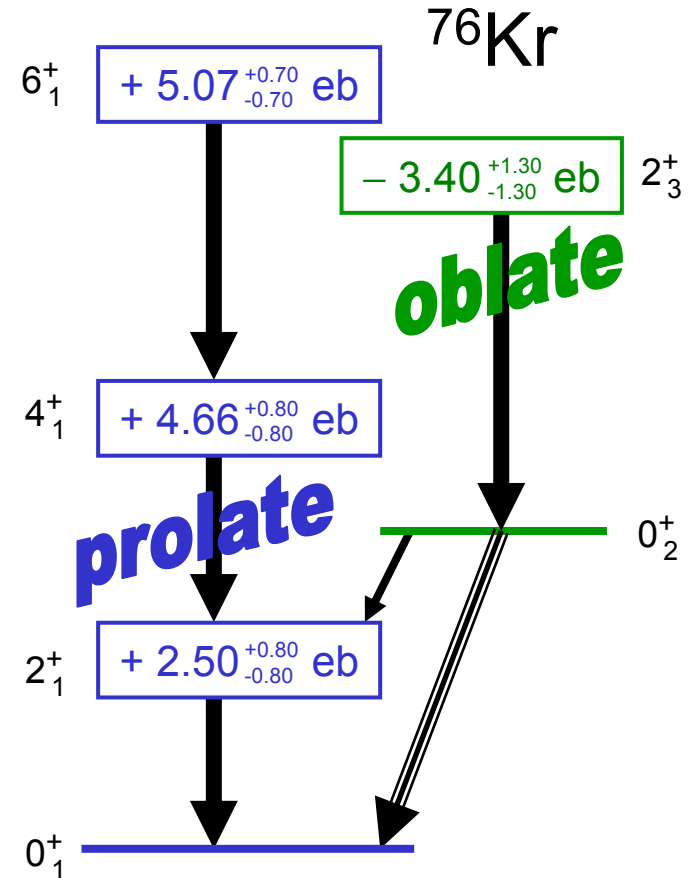
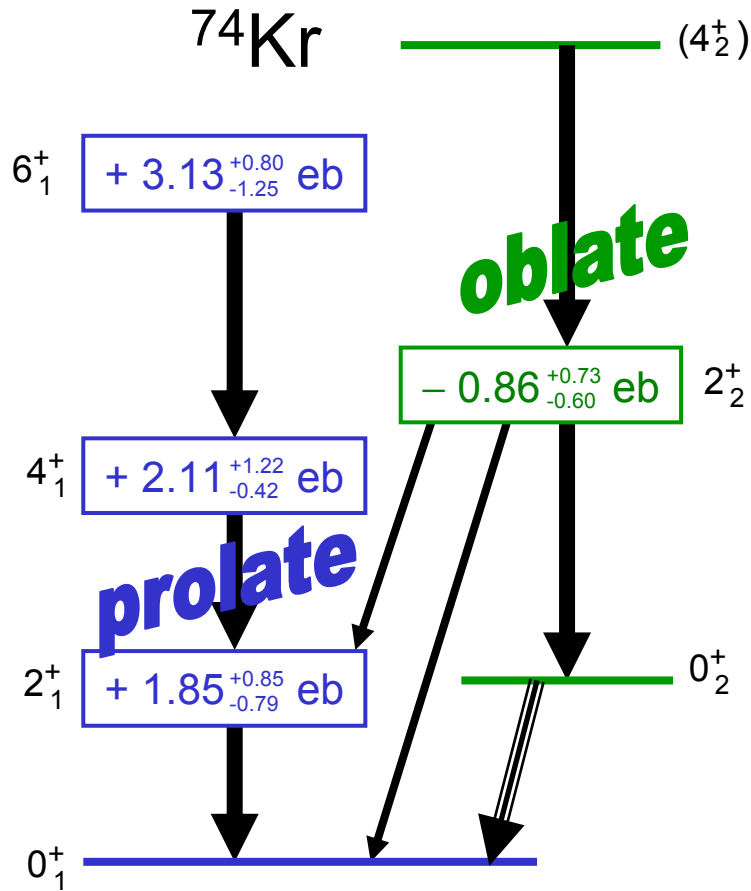
$$\langle 2_2^+ \| \mathbf{M}(E2) \| 2_2^+ \rangle = +0.33_{-0.23}^{+0.28}$$

positive matrix element  
(negative quadrupole moment  $Q_0$ )

$\Rightarrow$  oblate shape



# Quadrupole moments $Q_0$ in $^{74}\text{Kr}$ and $^{76}\text{Kr}$

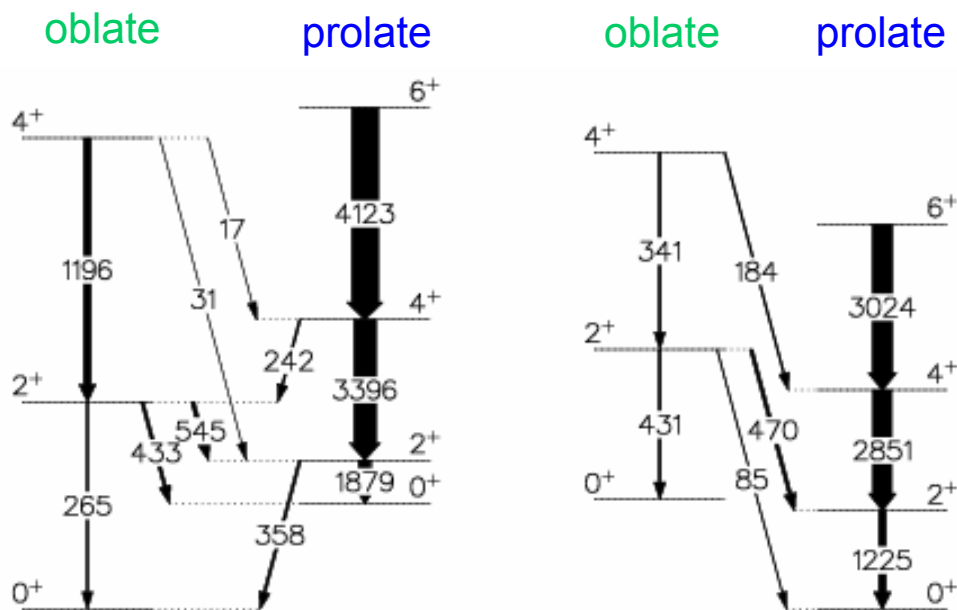


E. Clément et al., to be published

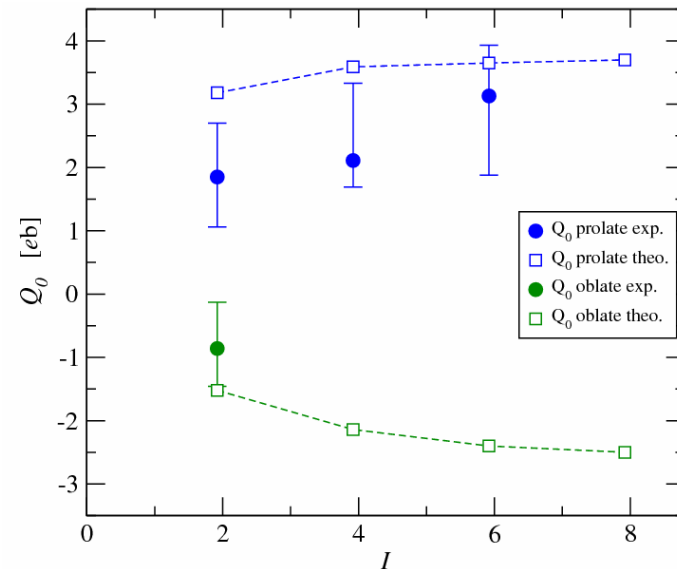
- direct confirmation of the prolate – oblate shape coexistence
- first reorientation measurement with radioactive beam

# Comparison with theory: $^{74}\text{Kr}$

B(E2) values in  $e^2\text{fm}^4$



Quadrupole moments



theory: HFB(SLy6) + GCM  
M. Bender, P. Bonche,  
P.-H. Heenen, priv. comm.

experimental

- ordering of prolate and oblate states inverted
- reduced strength of  $2^+ \rightarrow 0^+$  transition reproduced  $\Rightarrow$  mixing
- in-band B(E2) values and  $Q_0$  too large  $\Rightarrow$  deformation

# Summary

- low-energy projectile Coulomb excitation with RIB
  - transitional and diagonal matrix elements for  $^{74,76}\text{Kr}$
  - first reorientation measurement with RIB
- Plunger lifetime measurement after fusion-evaporation
  - complementary measurement of  $B(E2)$  values
- direct confirmation of shape coexistence in light Kr
  - quantitative understanding
  - important input for theory
- new program to study neutron-rich Ar isotopes
  - experiment on  $^{44}\text{Ar}$  successfully completed last week
  - stay tuned...

# Collaboration

**E. Clément**, E. Bouchez, A. Chatillon, A. Hürstel,  
W. Korten, Y. Le Coz, Ch. Theisen, J.N. Wilson

## **Saclay**

J.M. Casandjian, G. de France

## **GANIL**

T. Czsonyka, J. Iwanicki, P. Napiorkowski, M. Zielinska

## **Warsaw**

G. Sletten

## **NBI**

C. Andreoiu, P.A. Butler, R.-D. Herzberg, D.G. Jenkins, G.D. Jones

## **Liverpool**

F. Becker, J. Gerl

## **GSI**

W.N. Catford, C. Timis

## **Surrey**

A. Dewald, B. Melon, O. Möller, K.O. Zell,

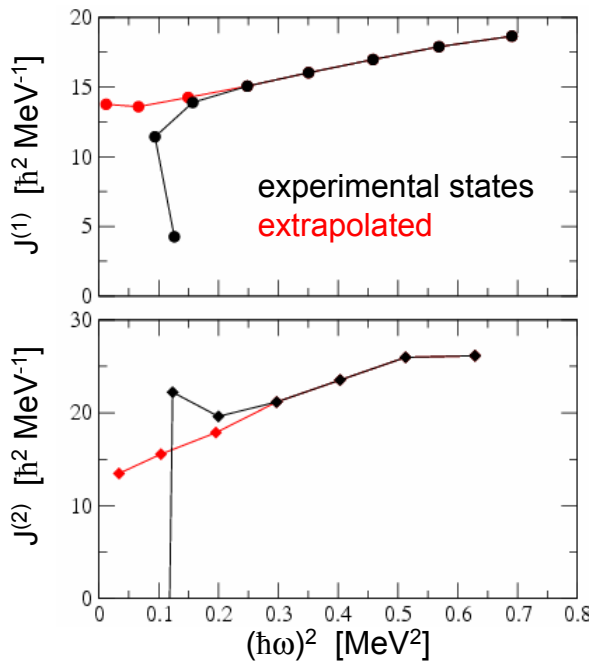
## **Köln**

N. Marginean, R. Menegazzo, D. Tonev, C.A. Ur

## **Legnaro**

fin

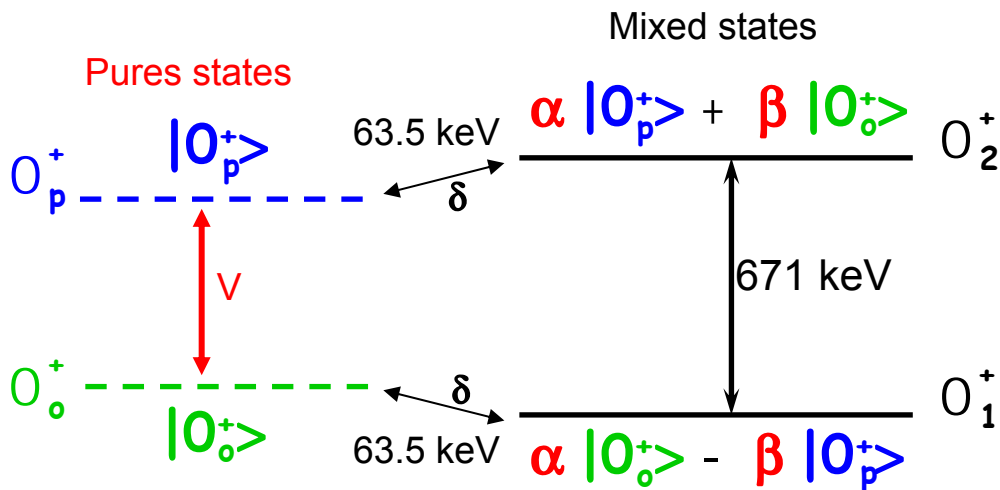
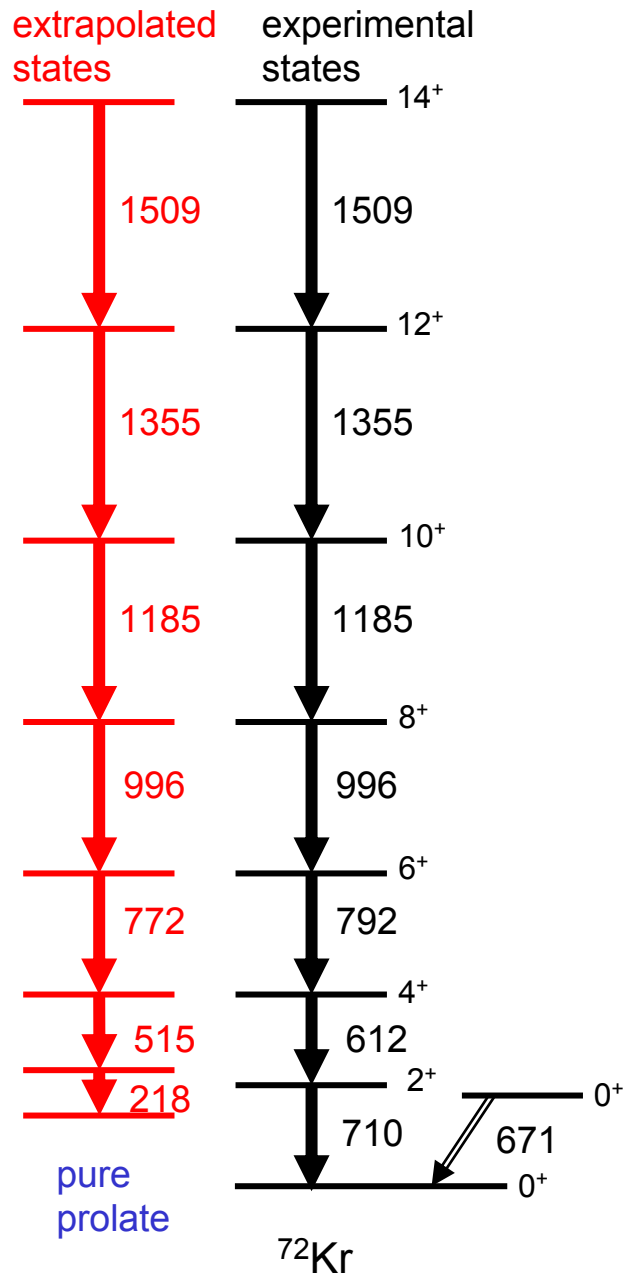
# Level mixing



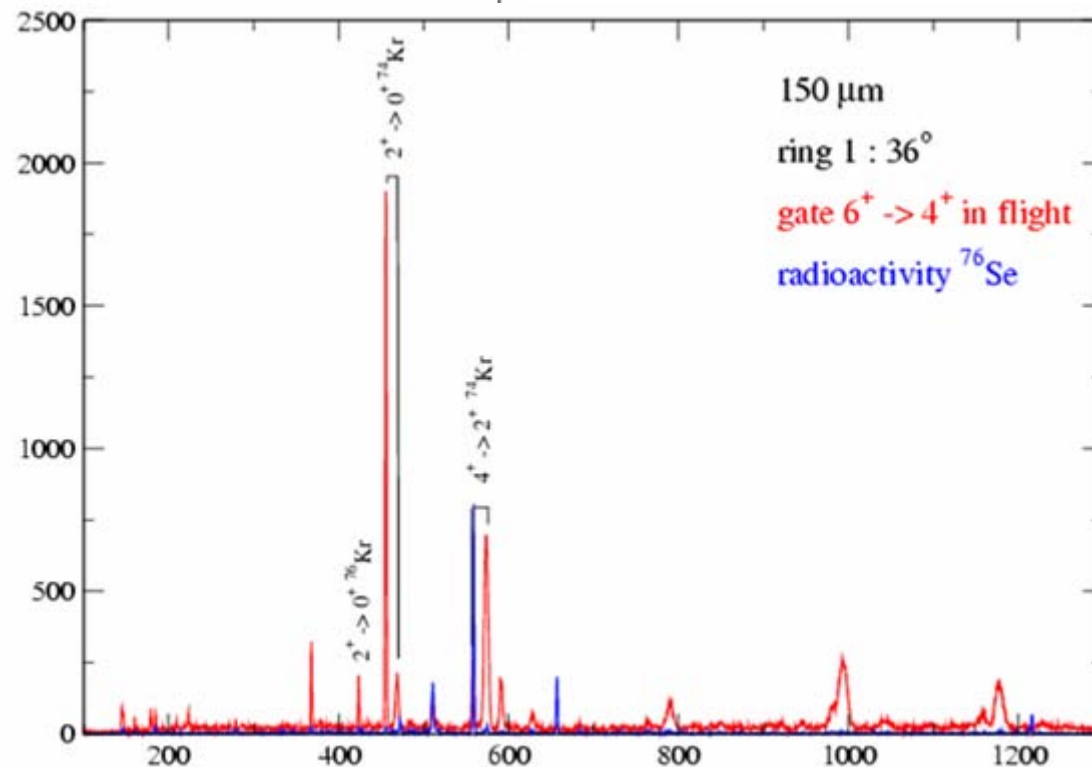
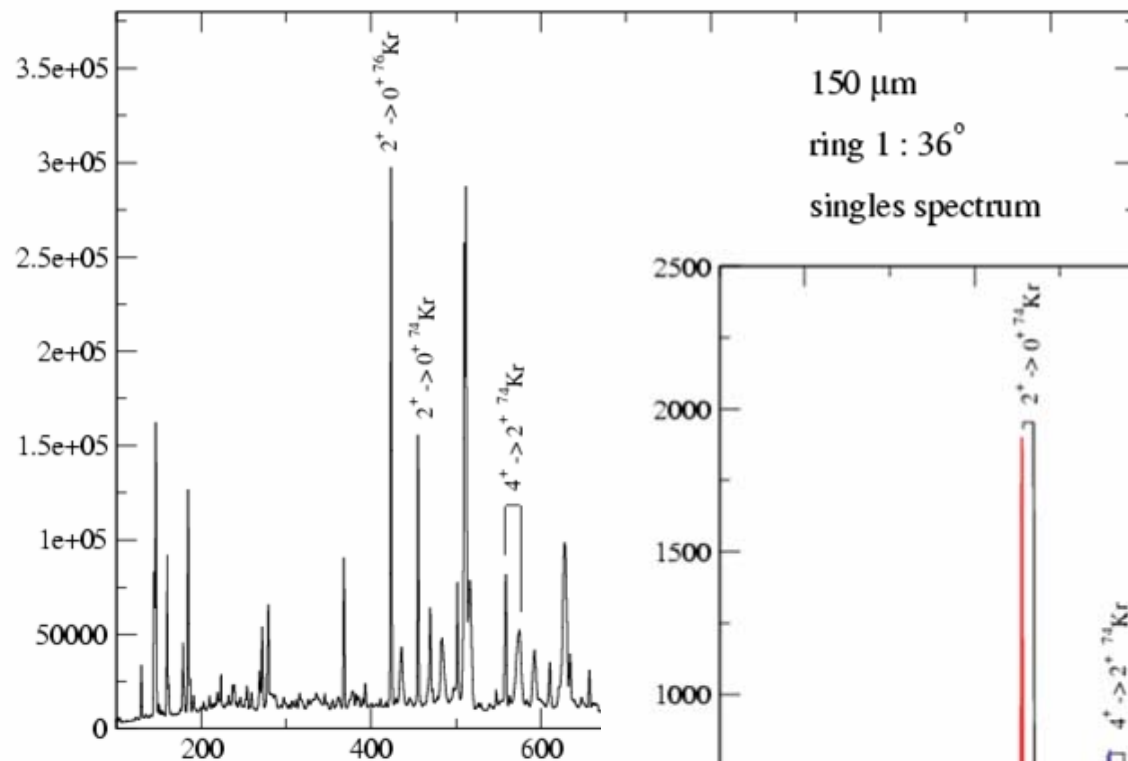
Regular rotational cascade at high spin.

Rotational band is distorted at low spin.  
 $\Rightarrow$  influence of mixing

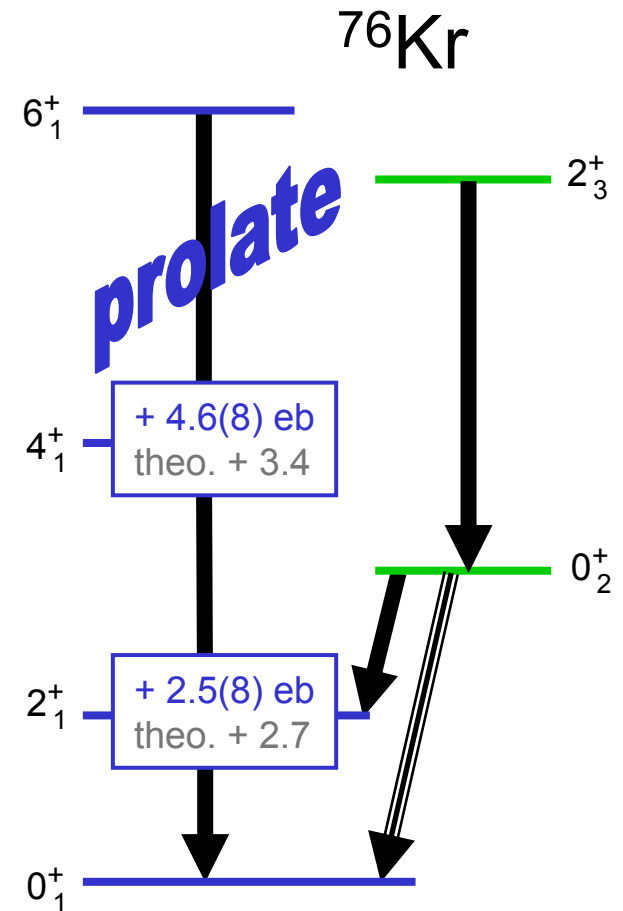
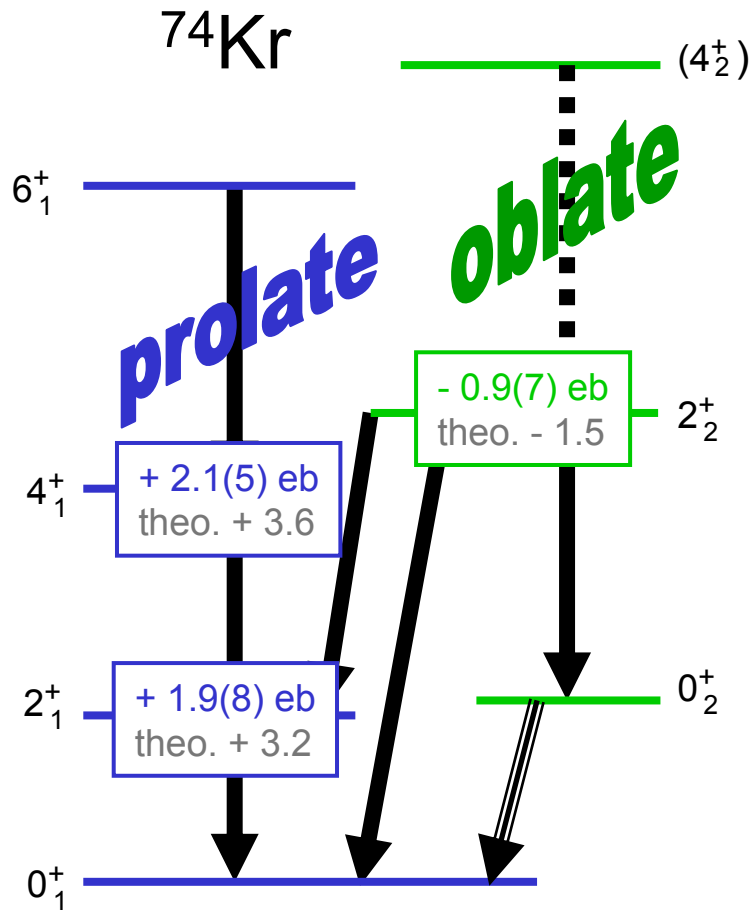
- $\triangleright$  Interaction  $V$
- $\triangleright$  mixing amplitudes  $\alpha, \beta$



# Singles vs. coincidence measurement



# Quadrupole moments in $^{74}\text{Kr}$ and $^{76}\text{Kr}$

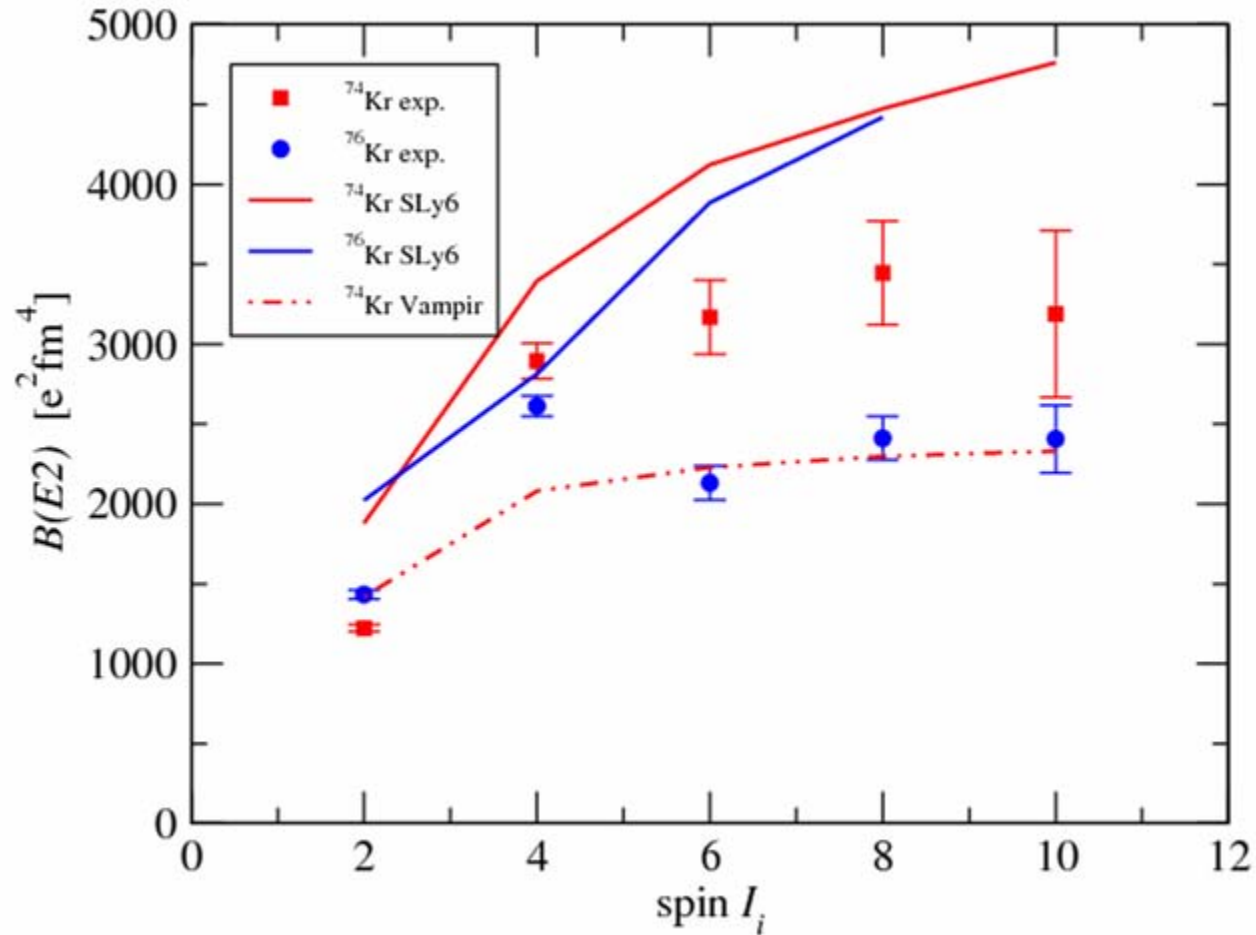


E. Clément et al., to be published

**direct confirmation of the prolate – oblate shape coexistence**



# Transition strengths : B(E2)

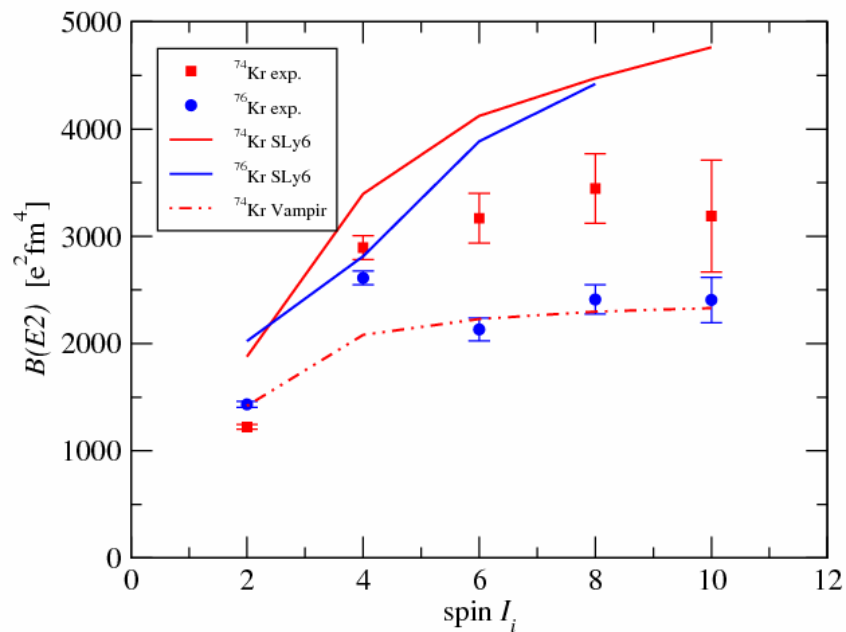
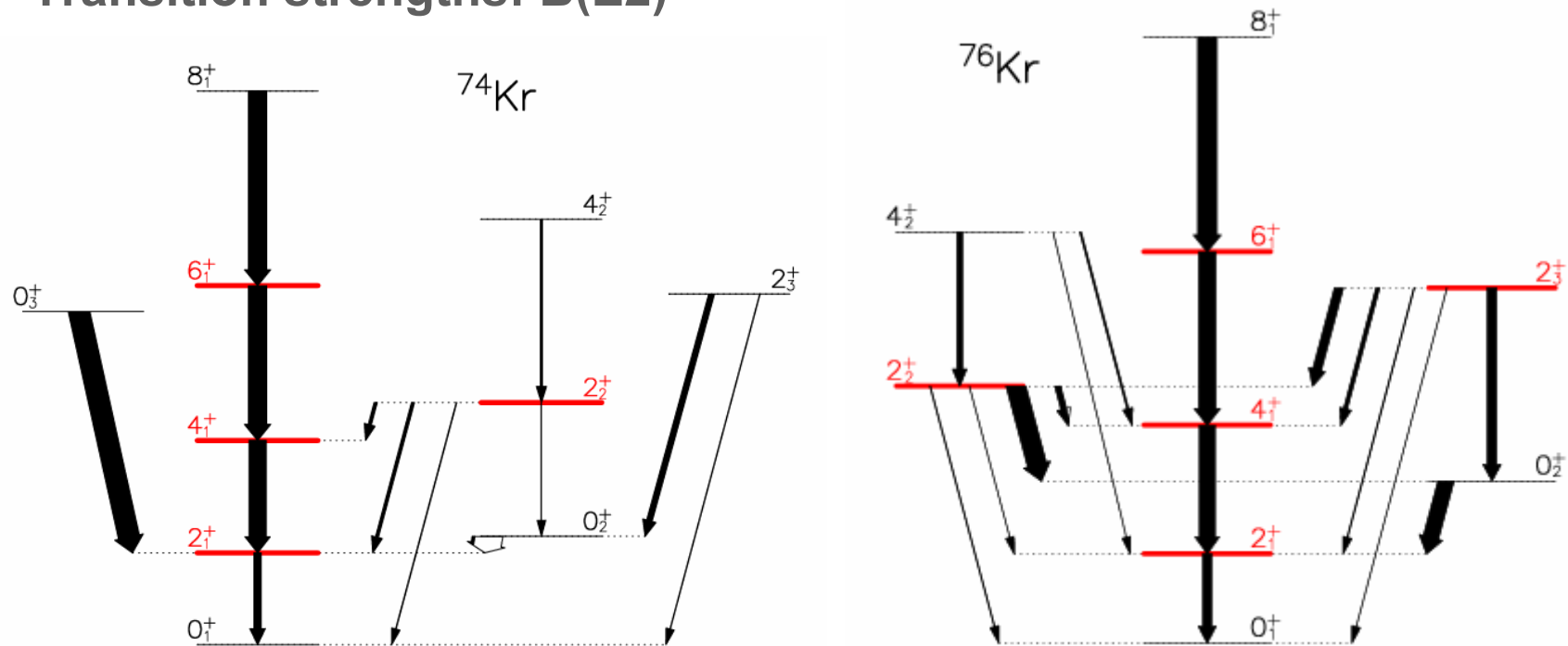


Theory:  
HFB+BCS-LN+AMPGCM  
M. Bender, P.H. Heenen  
priv. comm.

Vampir  
A. Petrovici et al.,  
Nucl. Phys. A 665, 333 (00)

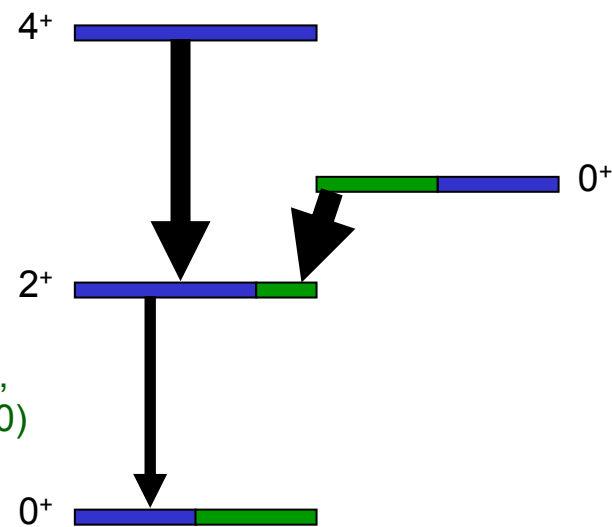
- B(E2) reduced for  $2^+ \rightarrow 0^+$  transitions  $\Rightarrow$  influence of mixing
- theory describes trend, but not absolute values

# Transition strengths: B(E2)

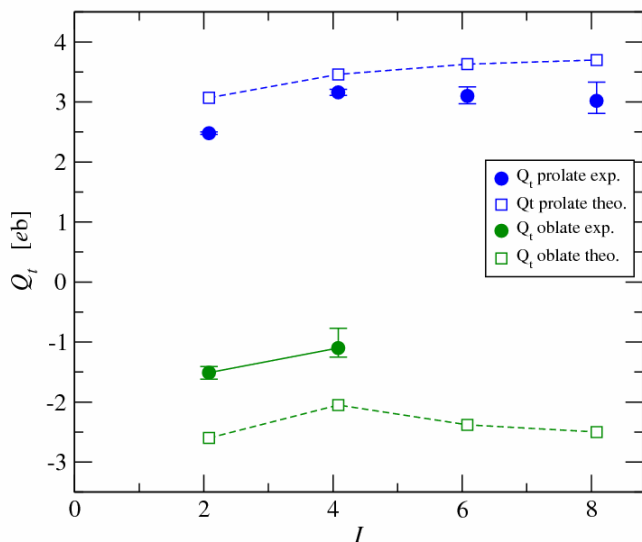
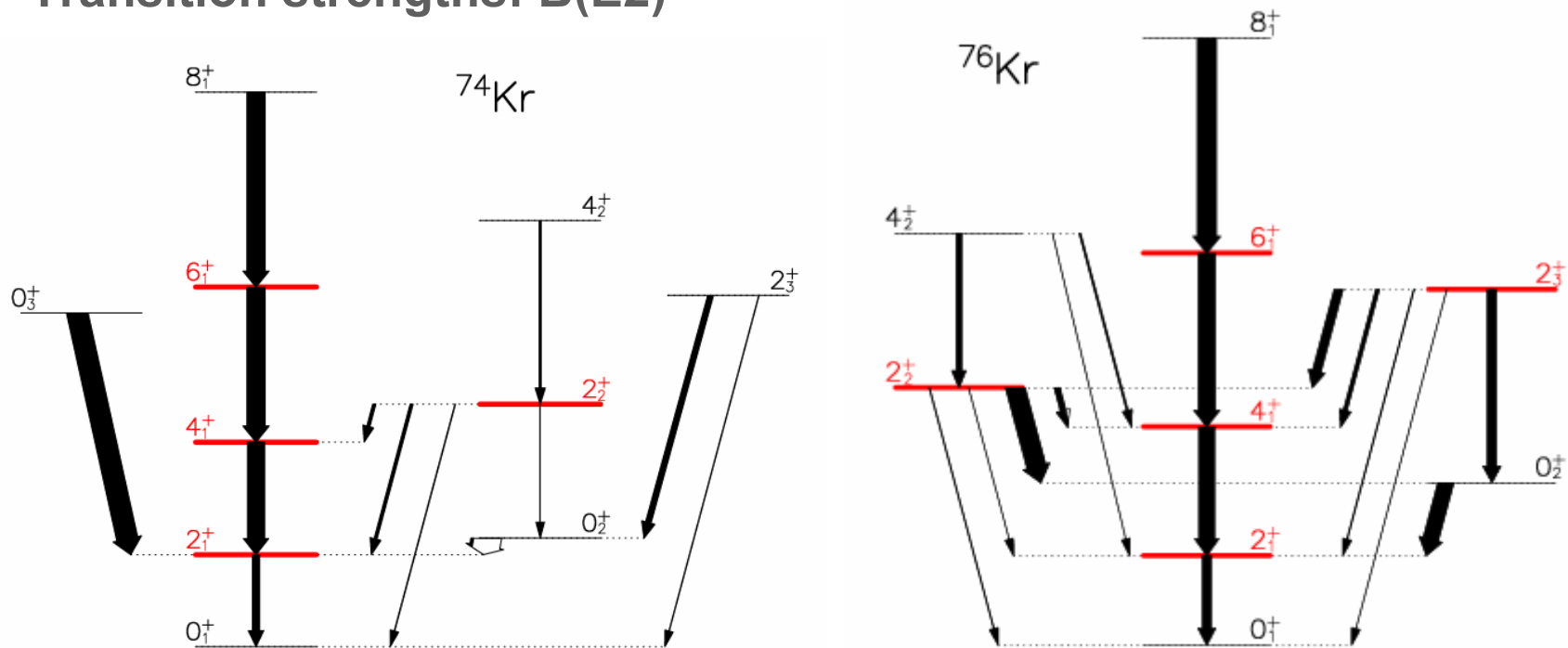


HFB+AMPGCM  
M. Bender,  
P.H. Heenen  
priv. comm.

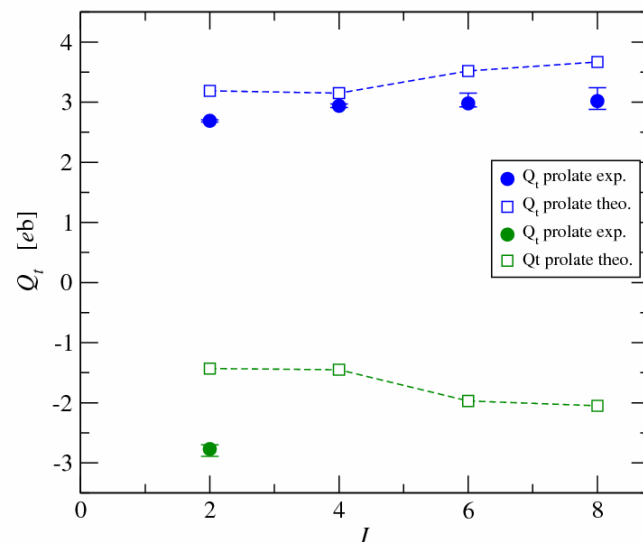
Vampir  
A. Petrovici et al.,  
NPA 665, 333 (00)



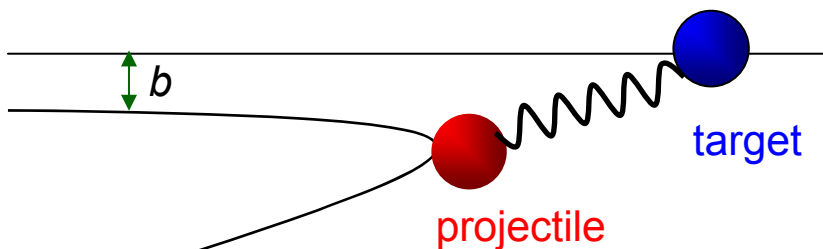
# Transition strengths: B(E2)



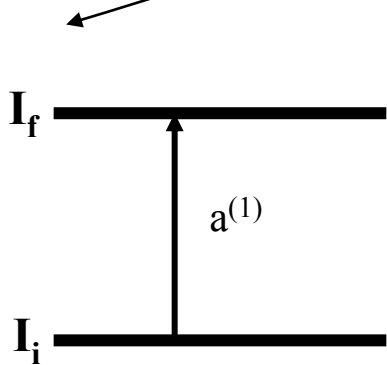
HFB+GCM  
M. Bender,  
P.H. Heenen  
priv. comm.



# Coulomb excitation

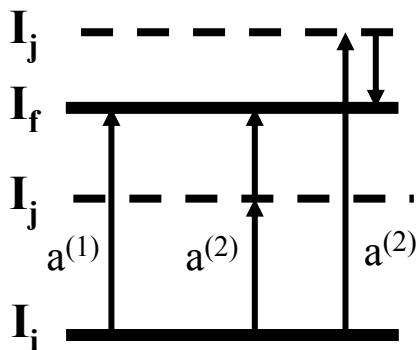


- safe energy:  $r_d > 1.25 (A_T^{\frac{1}{3}} + A_P^{\frac{1}{3}}) + 5$  fm
- purely electromagnetic process
- excitation cross section is a direct measure of the  $E\lambda$  matrix elements.



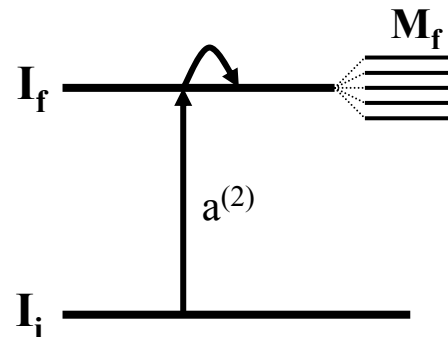
1<sup>st</sup> order:

$$a^{(1)} \propto \langle I_f \| M(E2) \| I_i \rangle$$



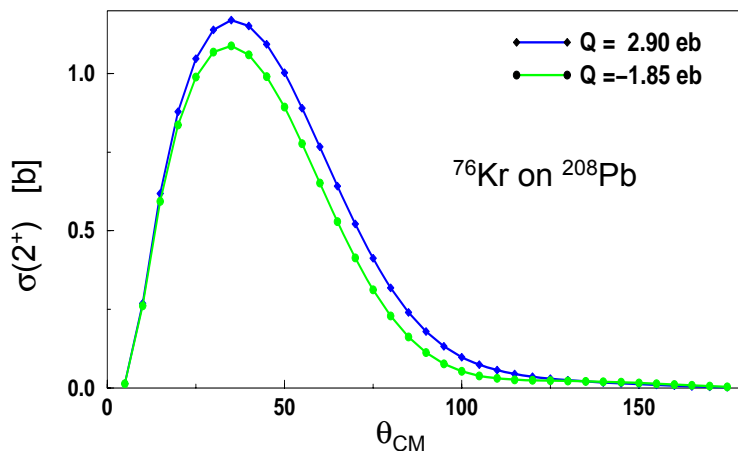
2<sup>nd</sup> order:

$$a^{(2)} \propto \sum_j \langle I_f \| M(E2) \| I_j \rangle \langle I_j \| M(E2) \| I_i \rangle$$



reorientation effect:

$$a^{(2)} \propto \langle I_f \| M(E2) \| I_f \rangle \langle I_f \| M(E2) \| I_i \rangle$$



sensitive to diagonal matrix elements  
 ⇒ intrinsic properties of final state:  
 quadrupole moment including sign